

MTH 201
Multivariable calculus and differential equations
Homework 10
First order ordinary differential equations

1. Solve each of the following differential equations

(a) $(x^2 - 2y^2)dx + xydy = 0.$

(b) $x \sin(y/x) \frac{dy}{dx} = y \sin(y/x) + x.$

(c) $(x + \frac{2}{y})dy + ydx = 0.$

(d) $(\sin x \tan y + 1)dx + (\cos x \sec^2 y)dy = 0.$

(e) $dx = \frac{y}{1-x^2y^2}dx + \frac{x}{1-x^2y^2}dy.$

(f) $xdy - ydx = (1 + y^2)dy.$

(g) $ydx - xdy = xy^3.$

(h) $x \frac{dy}{dx} - 3y = x^4.$

(i) $\frac{dy}{dx} + y = 2xe^{-x} + x^2.$

(j) $x \frac{dy}{dx} + y = x^4y^3.$

(k) $x \frac{dy}{dx} = 5y + e^{-2x}y^{-2}.$

2. Solve each of the following Initial value problems (IVPs)

(a) $\frac{dy}{dx} = e^{y-x} \sec(y) (1 + x^2), y(0) = 0.$

(b) $x \frac{dy}{dx} + 2y = x^2 - x + 1, y(1) = 1/2.$